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Geometry optimization of uncoated silicon microcantilever-based gas density sensors

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Abstract:

In the absence of coating, the only way to improve the sensitivity of silicon microcantilever-based density sensors is to optimize the device geometry. Based on this idea, several microcantilevers with different shapes (rectangular-, U- and T-shaped microstructures) and dimensions have been fabricated and tested in the presence of hydrogen/ nitrogen mixtures (H2/N2) of various concentrations ranging from 0.2% to 2%. In fact, it is demonstrated that wide and short rectangular cantilevers are more sensitive to gas density changes than U- and T-shaped devices of the same overall dimensions, and that the thickness doesn't affect the sensitivity despite the fact that it affects the resonant frequency. Moreover, because of the phase linearization method used for the natural frequency estimation, detection of a gas mass density change of 2 mg/l has been achieved with all three microstructures. In addition, noise measurements have been used to estimate a limit of detection of 0.11 mg/l for the gas mass density variation (corresponding to a concentration of 100 ppm of H2 in N2), which is much smaller than the current state of the art for uncoated mechanical resonators.

Keywords: Density sensor, hydrogen sensor, microcantilever, geometry optimization, sensitivity optimization, Euler-Bernoulli beam theory, hydrodynamic function.

1. Introduction

In recent years microcantilever-based chemical, biological and physical sensors have attracted the interest of numerous researchers due to their high surface-to-volume ratio and their high performance in both gas and liquid phases [1-6]. For chemical and biochemical sensing applications, the microcantilevers are usually coated with a sensitive layer whose purpose is to selectively sorb the analyte of interest, resulting in either a static deflection (bilayer effect) in the static mode or a shift in the resonant frequency (mass effect) in the dynamic flexural mode. Furthermore, it has been demonstrated that uncoated micro- or millimeter size cantilevers operated in the dynamic flexural mode exhibit good sensitivities to gas mass density [7,8], liquid mass density [9] and/or viscosity [10,11].

With a view towards chemical detection in gas media, the variation of the gas density can reflect the variation of a chemical species concentration in a gas mixture [8, 12-14]. The operating principle of an uncoated silicon microcantilever (USMC) used as a density or chemical sensor is based on the influence of the mass of the fluid moved by the vibrating cantilever on the resonant frequency. In fact, when the surrounding fluid mass density increases (decreases), the equivalent effective mass of the cantilever increases (decreases), thereby causing the resonant frequency to decrease (increase) [12].

The absence of a coating eliminates or significantly reduces several problems associated with microcantileverbased sensors such as long-time response, drift and aging effects. However, uncoated microcantilevers are nonselective and offer very low sensitivities, making it quite challenging to detect small concentration changes (small density changes). This last point serves as the motivation to increase the sensor sensitivity through geometry optimization.

In the literature geometry optimization has already been reported for other particular cases of chemical detectors. For example, in the static bending mode, A. Loui *et al.* [15] have studied the influence of the length-to-width aspect ratio on the sensitivity of rectangular cantilevers due to both surface stress and an end-force loading. They have found that structures with a low aspect ratio are better for surface-stress applications and structures with high aspect

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ratio are optimal for point-loading scenarios. In the case of dynamic mode operation, the cantilever mass sensitivity is proportional to its resonant frequency. The resonant frequency is proportional to the square root of the stiffness and inversely proportional to the square root of the effective mass. Therefore, the majority of the studies conducted in order to improve the mass sensitivity of cantilevers are focusing on increasing the stiffness (k) and/or decreasing the effective mass (meff) using different methods. H. Hocheng et al. [16] have demonstrated using different microcantilever shapes that the higher the structural stiffness is, the better the sensitivity is. Similarly, S. Subramanian et al. [17] suggested the use of a nonlinear width profile for V-shaped microcantilevers in order to increase the structural stiffness and subsequently the mass sensitivity. For bio-sensing applications and in order to improve the overall (static-mode and dynamic-mode) sensitivity of a microcantilever, as measured by the product of static deflection and resonant frequency, M.Z. Ansari et al. [18] proposed using a non-uniform cantilever cross-section (giving increased k and decreased *meff*) and reducing the fixed-end area (increasing the static deflection). The authors suggested triangular or step cross-section profiles instead the conventional rectangular one. Another solution, proposed by M. Narducci et al. [19], consisted of reducing the microcantilever size (increasing k and reducing *meff*) and/or using higher-order modes. In the case of end-mass loading, S. Morshed et al. [20] have demonstrated via simulation studies that structures with high aspect ratio (length-to-width) are more sensitive to local end-mass variation; furthermore, they have suggested the use of a triangular microcantilever shape to enhance the stiffness and minimize the effective mass at the free-end of the structure. Furthermore, to enhance the capabilities of microcantilevers in liquid media, L.A. Beardslee et al. [21] have studied the influence of the beam geometry on both the quality factor and the resonant frequency in a liquid medium (water) in order to limit the viscous damping effect, thus improving the detection limit of chemical sensing. The authors reported that the use of the in-plane bending mode reduces the damping and the mass loading due to the surrounding fluid, and that beams that are wide, thin and short and operated in the in-plane mode are more suitable for liquid-phase chemical detection.

As reported above, the resonant frequency is a key parameter in determining the cantilever mass sensitivity and all researches are

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focusing on enhancing this parameter. The microcantilever operating in fluidic (gas or liquid) environments interacts with the surrounding fluid which causes a distributed mass depending on the fluid properties, frequency and cantilever width [22]. Thus, although the resonant frequency is an important parameter to mass density sensing, the structure's geometry and dimensions play an important role in the mass density sensitivity of microstructures. In the present work we study the effect of microcantilever shape (rectangular, U- and T-shaped microstructures) and geometrical dimensions on the gas mass density sensitivity (i.e., the ratio of resonant frequency variation to the density variation). To perform this study several uncoated silicon microcantilever shapes with different dimensions have been designed and fabricated. The structures have been tested at room conditions using different concentrations (0.2-2.0%) of hydrogen (H_2) in nitrogen (N_2) . The density changes have been measured by monitoring the eigenfrequency (natural frequency) variation using the efficient phase linearization method [23].

2. Modeling

The Euler–Bernoulli equation taking into account the hydrodynamic force acting on the uncoated microcantilever is commonly used to model the behavior of resonating microcantilevers in fluid media when the influence of the beam's shearing deformation and rotational inertia can be neglected [8] and [12]. Fig. 1 displays the out-of-plane cantilever flexural mode (w is the free-end transverse deflection) and the geometric parameters: length (L), width (b) and thickness (h).



Fig.1: Schematic representation of both the microcantilever geometry and the transverse bending deflection (*w*). The beam dimensions are width (*b*), length (*L*) and thickness (*h*).

In this work, the Euler–Bernoulli model in a fluid medium is used to characterize the changes in structural behavior due to the gas density variation. This model is valid only when [22]

- The beam has a uniform cross-section (geometry and materials) along the structure.
- The cross-sectional dimensions are negligible compared to the length of the structure: *h* « *b* « *L*.
- The deflection is negligible compared to the structural dimensions: *w* < *h*.

The solution of the differential equation governing the cantilever's motion in the presence of a surrounding fluid gives [22] and [24]:

$$\frac{df_0}{f_0} \simeq \frac{df_0}{f_{0,vac}} = -a_0 \frac{\pi}{8} \frac{b}{h} \frac{\rho_f}{\rho} \frac{d\rho_f}{\rho_f} \tag{1}$$

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with

$$f_{0,vac} = \frac{\lambda_n^2 h}{2\pi L^2} \sqrt{\frac{E}{12\rho}}$$
(2)

being the natural frequency in vacuum and f_0 the in-fluid natural frequency. Symbols *E* and ρ denote the Young's modulus and density of silicon, ρ_f is the fluid density, λ_n is a coefficient depending on the eigenfrequency mode [25] ($\lambda_1 = 1.875$, $\lambda_2 = 4.695$, $\lambda_3 = 7.854$, etc.), and $a_0 = 1.0553$. The latter parameter is associated with an approximation introduced by Maali et al. [24].

The absolute density sensitivity of resonating sensors is defined as the ratio between the resonant frequency variation and the density variation. Based on Eqs. (1) and (2), the absolute sensitivity can be written as

$$S_a = \left| \frac{\Delta f_0}{\Delta \rho_f} \right| = \frac{a_0}{\rho} \frac{b}{L^2} \frac{\lambda_n^2}{16} \sqrt{\frac{E}{12\rho}}$$
(3)

According to Eq. (3), it can be observed that the sensitivity of a rectangular beam, based on the Euler–Bernoulli assumption, depends only on two geometric parameters –- width (*b*) and length (*L*) –- and does not depend on the thickness (*h*). This result shows that changes in sensitivity need not be accompanied by changes in the resonant frequency. For example, increasing the width increases the sensitivity but does not affect the resonant frequency. It is expected from this equation that shorter and wider cantilevers will yield higher values of absolute sensitivity S_a . Of course, the range of applicability of Eq. (3) is limited to that of the Euler–Bernoulli theory on which it is based. Thus, an extreme reduction in length *L* would need to be accompanied by a corresponding reduction in thickness *h* in order to maintain the validity of Eq. (3); otherwise, the effects shear deformation and

rotational inertia, neglected in elementary beam theory, will become important. Such a reduction in h will also serve a more practical purpose: the use of shorter and wider cantilevers, which by Eq. (3) will improve the absolute sensitivity, will eventually become too stiff to render a measurable signal; reducing h will help to delay the onset of this practical limit to the applicability of Eq. (3).

3. Experiments

In order to experimentally study the optimization of the sensor sensitivity, several microcantilevers with different geometries (rectangular-, U- and T-shaped microstructures) and dimensions (L, b and h) have been fabricated (Fig. 2b; Table 1) with electromagnetic actuation and piezoresistive read-out (Fig. 2a).



Fig.2: (a) Uncoated silicon microcantilever design: (1) Printed Circuit Board, (2) adhesive, (3) silicon, (4) constant magnetic field, (5) metal, (6) AC current, (7) piezoresistor and (8) AC Lorentz force. (b) Different microcantilever geometries (rectangular-, U- and T-shaped) and geometric parameters: total length 'L', total width 'b', thickness 'h', leg length 'Lleg' and leg width 'bleg'.

	[n	ım]		[µm]	[mm ²]	
Specimen	L	b	h	L_{Leg}	b_{Leg}	Surface
U1_5µ	1	1	5	666	250	0.670
U2_5µ	1	1	5	333	250	0.830
T1_5µ	1	1	5	500	200	0.600
Τ2_5μ	1	1	5	250	200	0.800
A0_5µ	0.5	0.25	5	-	-	0.125
A1_5µ	0.5	0.5	5	-	-	0.250
A2_5µ	1	1	5	-	-	1.000
A2_10µ	1	1	10	-	-	1.000
A3_5µ	2	1	5	-	-	2.000

Table 1: Microcantilever dimensions and surface areas. Extensions " $_5\mu''$ and " $_10\mu''$ indicate the specimen thickness in μ m.

A gas line [23] has been used to generate different concentrations of H₂ in N₂ and to control the gas mixture flow. The different gas densities (ρ_{H2-N2}), gas density variations ($\Delta \rho_{H2-N2}$) and relative gas density variations ($\Delta \rho_f / \rho_f$) of the gas fluid (H₂-N₂) corresponding to different concentrations of H₂ in N₂ are reported in Table 2.

Concentrations of H ₂ in N ₂ (%)	$ ho_{H2-N2}$ (kg.m ⁻³)	$\Delta \rho_{H2-N2}$ (kg.m ⁻³ or g/l)	$\Delta \rho_f / \rho_f = \Delta \rho_{H2-N2} / \rho_{N2} (\%)$
100	0.0830	-1.0703	-93
2	1.1314	-0.0214	-1.8
1	1.1421	-0.0107	-0.93
0.6	1.1464	-0.0064	-0.56
0.2	1.1506	-0.0021	-0.19
0	1.1533	0	0

Table 2: Densities (ρ_{H2-N2}), density variations ($\Delta \rho_{H2-N2}$) and relative density variations ($\Delta \rho_{f}/\rho_{f}$) corresponding to different concentrations of H2/N2 gas mixture. These values are calculated at room conditions (23°C and 1.01325 bar).

3.1. Actuation and read-out systems

To actuate the cantilevers (Fig. 2a), an AC current is passed through the conductive loop wire placed along the cantilever periphery. In the presence of a magnetic field collinear to the longitudinal axis of the beam, an AC Lorenz force is created at the microcantilever free-end and induces out-of-plane vibrations (Fig. 1). Semiconductor strain gauges which are boron-doped piezoresistors have been fabricated during the process in order to read-out the vibrations. They are arranged in a half Wheatstone bridge configuration: a first gauge is located at the clamped-end of the beam where the strain is maximum and the second one is on the rigid substrate.

3.2. Microcantilever fabrication

The main steps of the fabrication process are as follows. The starting substrate was a 100 mm-diameter, $~\langle 1~0~0 \rangle$, N-type silicon-

on-insulator (SOI) wafer, with a 1 μ m-thick buried oxide and a 5 μ mthick (or 10 μ m-thick) top silicon layer (resistivity of 4–6 Ω cm). The use of the SOI wafer enabled the precise control of the cantilever thickness, ensuring the consistency of their mechanical properties. The first step consisted of creating the piezoresistor in the bulk silicon. In order to optimize the piezoresistor sensitivity, the cantilevers were patterned along crystal axes for which the longitudinal piezoresistive coefficient is maximum, i.e., along the $\langle 1 \ 1 \ 0 \rangle$ direction in the case of a *p*-silicon piezoresistor. The fabrication method relied on the implantation of germanium (Ge) and boron fluorine (BF₃) in order to obtain an ultrathin piezoresistor [26]. The localization of the piezoresistive layer at the anchored edge of the cantilevers was achieved by using silicon dioxide as a masking layer. For that purpose, 300 nm of silicon dioxide was thermally grown and patterned with a photolithographic step. Germanium was implanted with an energy of 60 keV and a dose of 5×10^{14} ions/cm² through a 6-nm silicon dioxide layer to create a preamorphized layer. This layer avoided channeling effects during the boron implantation and led to a very thin doped region. Boron fluorine was then implanted with an energy of 15 keV and a dose of 1×10^{16} ions/cm². Owing to the heavier mass of the BF₃ molecules relative to boron, the use of BF₃ resulted in a thickness reduction of the p⁺-doped region. The implantation process was followed by rapid thermal annealing at 1000 °C for 15 s to minimize boron diffusion during the recrystallization of the amorphized layer and the electrical activation. This was followed by conventional annealing at 850 °C during 20 min. The next step consisted of the deposition of 200 nm of plasma enhanced chemical vapor deposition (PECVD) silicon dioxide on the entire SOI wafer before the sputtering of aluminum (AI) (500 nm) for the electrode used for electromagnetic actuation. The oxide prevented shortcircuiting between the piezoresistors and the actuation electrodes. Lift-off of the Al film was achieved by using an AZ nLOF negative photoresist to define the electrodes. A passivation silicon oxide film (200 nm thick) was then deposited by PECVD. Contact pads were opened by dry etching of PECVD-deposited oxide. To finish, the microcantilever shapes were defined by a front reactive ion etching of silicon, followed by vertical sidewalls etching on the backside of the SOI wafer using the deep reactive ion etching technique to release the structures. The 1 μ m-thick SiO₂ acted as an etch stop layer for the dry silicon etching. This layer was then removed by Reactive ion etching. The resulting microstructural shapes, dimensions and surface areas are reported in Table 1.

3.3. Experimental setup

With the aim of comparing the different microcantilever geometries and dimensions in terms of sensitivity to density variation, measurements of various H₂ in N₂ concentrations (0.2, 0.6, 1 and 2%) have been performed using a gas line with a flow of 100 ml/min. The hermetic cell containing the tested microcantilever had a volume of 500 µl. A gain/phase analyzer (HP4194A) controlled with a *LabVIEW* program was used to acquire the phase spectrum every nine seconds (1 acquisition/9 s). In order to measure the natural frequency variation (Δf_0), a linearization of the phase spectrum around the resonance was used to extract the natural frequency (f_0) as detailed in [23].

The study of both the geometry and the size influence on the sensor sensitivity was performed with tests using the first resonant mode of each structure. The first step of the study consisted of determining the structural shape influence (rectangular-, U- or T-shaped) by comparing the sensitivities of the structures A2_5 μ , T1_5 μ , T2_5 μ , U1_5 μ and U2_5 μ , all having the same total length (*L*), total width (*b*) and thickness (5 μ m). The second step involved an investigation of the influence of the dimensions (*L*, *b* and *h*) on the sensitivity for the best sensitive shape (geometry) revealed by the results of the first step. An example of the measurement performed for each microstructure of Table 1 is presented in Fig. 3.



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Fig. 3: Example of detection curve obtained using A2_5 μ structure with different concentrations of H₂ in N₂ with a gas flow of 100 ml/min at room conditions (Temperature≈23°C, pressure≈1 atm).

The optimization was performed by consideration of the absolute sensitivity defined in Eq. (3). Other sensor characteristics and performance metrics were also determined using the hydrogen detection measurements:

- The sensor noise (*Noise*) has been estimated by the standard deviation on the stabilized natural frequency ($\Delta f_0 \approx 0$)
- The signal-to-noise ratio (*SNR*) and the eigenfrequency variation (Δf_0) have been calculated at 1% of H₂ in N₂.
- The limit of detection (*LOD*) has been estimated: it corresponds to a signal-to-noise ratio equal to 3.
- The absolute sensitivity is the slope of the fitted line of the experimental measurements.

4. Results and discussion

4.1. Experiment set #1: influence of the shape

This first experiment set was used for the first step of the sensitivity study consisting of the examination of the shape influence (rectangular-, T- or U-shaped structure) on the sensitivity. Fig. 4a and b shows the experimental measurements (markers) and the fitting lines of the first-mode natural frequency variation as a function of H₂ in N₂ concentration and density variation, respectively. The A2_5µ structure has the highest sensitivity (slope) among all of the other structures considered, namely U1_5µ, U2_5µ, T1_5µ and T2_5µ. The performance metrics are presented in Fig. 4c and the numerical results are reported in Table 3.

This preliminary result allows us to conclude that for structures having the same total length (L), the same total width (b) and the same thickness (h), structures having more contact area (Table 1) with the surrounding fluid have the best absolute sensitivity (S_a) to the density variations of the surrounding gas (Fig. 4b; Table 3). This is a simplistic conclusion because structures having more contact area and keeping the same total length (L), total width (b) and total thickness

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(*h*), also have higher resonant frequency. According to these first experiments, we can conclude that the rectangular shape (A2_5 μ in these experiments) is the best geometry in terms of sensitivity for gas density sensing applications. It can be seen in Fig. 4c that the A2_5 μ structure also has the best quality factor (*Q*) and the best signal-to-noise ratio (*SNR*) and, thus, the best limit of detection (*LOD* = 100 ppm or 0.11 mg/l).



Fig. 4: Results of the first experiments. (a) Natural frequency variation as function of H₂ in N₂ concentration (0, 0.2, 0.6, 1 and 2%). (b) Natural frequency variation as function of the density variation of the H2-N2 gas mixture. (c) Performance of structures A2_5 μ , U1_5 μ , U2_5 μ , T1_5 μ and T2_5 μ in terms of natural frequency (f_0), quality factor (Q), natural frequency variation (Δf_0) at 1% of H₂ in N₂, noise (*Noise*) estimated by the calculation of the standard deviation, signal-to-noise ratio (*SNR*) calculated at 1% of H₂ in N₂, absolute sensitivity (S_a) which is the slope of the linear characteristics and limit of detection (*LOD*) in terms of H₂ in N₂ concentration (%) and density variation (mg.l⁻¹).

Specimen	f_{θ} (Hz)	Q	Δf_{θ} (Hz)	Noise (mHz)	SNR	$\frac{S_a}{(\text{Hz.kg}^{-1}.\text{m}^3)}$	LOD (%)	LOD (mg.l ⁻¹)
Α2_5μ	7082	120	1.28	4.43	289	117	0.01	0.11
U2_5µ	4580	94	0.80	4.1	195	73	0.015	0.16
U1_5µ	4624	90	0.58	3.6	161	53	0.019	0.20
Τ2_5μ	3480	92	0.56	3.80	147	53	0.02	0.22
T1_5μ	3431	90	0.45	3	150	42	0.02	0.21

Table. 3 : Numerical values of performance metrics extracted from the experiments made with A2_5 μ , U2_5 μ , U1_5 μ , T2_5 μ and T1_5 μ structures.

4.2. Experiment set #2: influence of the dimensions

The previous experiments have shown that, for the same overall dimensions, the rectangular structures are the best geometries in terms of sensitivity to the gas density changes. In this section we therefore study the effect of the geometric parameters (L, b and h) on the sensitivity of rectangular structures by analyzing the structural responses to the different concentrations of H₂ in N₂.

4.2.1. Thickness influence

The structures A2_5 μ and A2_10 μ have the same length and width (*L*, *b*) with thicknesses (*h*) of 5 μ m and 10 μ m, respectively. The detection curves of both structures are presented in Fig. 5a and b where it can be seen that thickness has no effect on the absolute sensitivity (*S*_a) (red triangle and green diamond markers). The fact that the absolute sensitivity is independent on the thickness is consistent with Eq. (3). Furthermore, doubling the thickness doubles the quality factor as can be seen in Table 4.

4.2.2. Length and width influence

Keeping in mind that the primary goal is to identify the best structure in terms of sensitivity to gas density, this part has three objectives:

Objective 1 consists of comparing the geometries A2_5µ and A3_5µ in terms of their absolute sensitivity (S_a). These structures have been selected because they have the same

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widths and thicknesses, but A3_5 μ is two times longer than A2_5 μ .

- Objective 2 involves the sensitivity comparison between the geometries $A1_5\mu$ and $A0_5\mu$ having the same lengths and thicknesses, but $A1_5\mu$ is two times wider than $A0_5\mu$.
- Objective 3 is to compare sensitivities of the two square geometries A1_5µ and A2_5µ having the same thickness, but the second structure has length and width two times larger than the first one.

The structural dimensions are reported in Table 1. Fig. 5 summarizes the detection results obtained with the different geometries and Table 4 reports the numerical characteristics and performance metrics of the different sensors. Performing in order the three comparisons mentioned above, the experimental results demonstrate the following:

- For a fixed width, the shorter beams have higher absolute sensitivities.
- For a fixed length, the wider beams have higher absolute sensitivities.
- When the width and length are both halved, the structure's sensitivity is increased by a factor of approximately two.

These points confirm the scale effects indicated by Eq. (3), which shows that the absolute sensitivity is proportional to the ratio of width to the square of the length (b/L^2) .



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Fig. 5: Results of the second set of experiments. (a) Natural frequency variation as function of H₂ in N₂ concentration (0, 0.2, 0.6, 1 and 2%). (b) Natural frequency variation as function of the density variation of the H₂-N₂ gas mixture. (c) Performance of structures A1_5 μ , A0_5 μ , A2_10 μ , A2_5 μ and A3_5 μ in terms of: natural frequency (f_0), quality factor (Q), natural frequency variation (Δf_0) at 1% of H₂ in N₂, noise (*Noise*) estimated by the calculation of the standard deviation, signal-to-noise ratio (*SNR*) calculated at 1% of H₂ in N₂, absolute sensitivity (S_a) which is the slope of the fitted straight lines and limits of detection (*LOD*) in terms of H₂ in N₂ concentration (%) and density variation (mg.l⁻¹).

Specimens	f_{θ} (Hz)	Q	Δf_{θ} (Hz)	Noise (mHz)	SNR	$\frac{S_a}{(\text{Hz.kg}^{-1}.\text{m}^3)}$	LOD (%)	LOD (mg. Γ^{-1})
Α0_5μ	41700	570	1.40	22.83	61	145	0.049	0.52
A1_5µ	27099	250	2.50	12.60	198	228	0.015	0.16
Α2_5μ	7082	120	1.28	4.43	289	117	0.010	0.11
Α2_10μ	11260	240	1.38	9.55	145	123	0.021	0.22
A3_5μ	1760	60	0.43	6.77	64	39	0.047	0.51

Table. 4: Numerical performance values extracted from the experiments made with A0_5 μ , A1_5 μ , A2_5 μ , A0_10 μ and A3_5 μ structures.

We note that all structures (experiment sets #1 and #2) detect 0.2% of H₂ in N₂, corresponding to 2 mg/l as density variation. Furthermore, we announce a theoretical detection limit (*LOD*) of 0.01% (100 ppm) of H₂ in N₂ corresponding to 0.11 mg/l as density variation for the A2_5µ structure, which is 800 times smaller than the published value of Rosario et al. [7]. We also note that this limit of detection can be improved considerably by increasing the actuation force.

4.3. Theory vs. experiment

In the literature there are no theoretical models that permit one to accurately predict the resonant frequency variation due to fluid density change for the case of complex geometries such as T-shaped, U-shaped and V-shaped cantilevers. The only existing model concerns parallelepiped-cantilever (rectangular) geometries that respect the Euler–Bernoulli conditions listed in Section 2. Therefore, only rectangular-shaped microcantilevers are considered for this comparison although their dimensions do not always respect the Euler–Bernoulli conditions.

In Fig. 6 comparisons are made between the model [Eqs. (1) and (2)] and measurements of natural frequency (f_0) and natural frequency variation (Δf_0) at 1% of H₂ in N₂.

We observe in Fig. 6a that the accuracy of the theoretical model in terms of f_0 estimation is satisfactory with the exception of the A0_5µ structure having a relative error of 25%. This error is most likely due to the structure etching defects [27] which have substantially modified the length of the cantilever (reduction). The evidence is provided by the fact that the structure A3_5µ, having exactly the same shape (L = 2b) as the A0_5µ structure but with a size four times larger (Table 1), shows good agreement between measurement and theory.

It can be observed in Fig. 6b that the relative deviation between model and measurement for the frequency shift estimation is about 50% for all structures except A3_5 μ . These relatively high deviations are due to the fact that the microcantilevers do not respect the Euler-Bernoulli conditions; thus, the fluid-structure interaction model proposed by Sader et al. [22] is not expected to give a good approximation. The A3_5 μ structure is two times longer than its width (L = 2b) and therefore has a smaller relative deviation (31%) than the other cases since the model is expected to be more applicable for longer geometries. The A0_5 μ structure has a larger error (46%) than A3_5 μ (31%) for the same reason mentioned in the previous paragraph.



Fig. 6: Comparison between model and measurements at 1% of H₂ in N₂. (a) Natural frequency (f_0). (b) Natural frequency variation (Δf_0).

In order to verify the effect of geometry in modeling accuracy, another measurement has been realized at the same room conditions (temperature = 23 °C, pressure = 1 atm) and gas conditions (H₂–N₂: 0.2–2%, gas flow = 100 ml/min) using another microcantilever ($L \times b \times h = 2000 \ \mu m \times 400 \ \mu m \times 5 \ \mu m$) having a length five times greater than its width ($L = 5 \times b$).

The frequency-shift results of this experiment are reported in Fig. 7 from which we see that the relative deviation between the model and the measurement for 1% of H₂ in N₂ is 3.12%. This result confirms that the Euler–Bernoulli conditions must be respected in order to achieve a good estimate using Sader's model [22] (or any model based on elementary beam theory). We also remark that the error increases for lower concentrations (0.6% and 0.2% in Fig. 7). The reason is the relatively large frequency step between each measurement caused by the relatively large span measurement in this case (20 Hz). In fact, the gain-phase analyzer (HP4194A) has a maximum of 400 measurement points; thus, configuring a span measurement of 20 Hz for the acquisition of the gain and phase spectra, a 50-mHz frequency step is achieved. However, using the phase linearization method [23], the resonant frequency can be estimated with a better accuracy than the frequency step.



Fig. 7: Measurement of concentration of H₂ in N₂ (0.2-2%) with gas flow of 100 ml/min using rectangular-shaped microcantilever ($L \ge b \ge h = 2000 \ge 400 \ge 5\mu m^3$). The triangle markers present experimental measurements, the blue line presents the theoretical modeling [Eq. (3)] and the red numerical values present the relative deviation between model and measurements.

5. Conclusions

We have demonstrated that uniform rectangular cantilevers are more suitable for density measurement than the other tested T- and U-shapes. Moreover, wide and short beams are more sensitive to the density variation, with the sensitivity of the rectangular beams being proportional to b/L^2 . Furthermore, the thickness does not affect the sensitivity of rectangular cantilevers to the mass density changes despite the fact that it affects the resonant frequency. However, the noise on the resonant frequency estimation depends on the thickness of the microcantilever. Thus, in order to select the most appropriate thickness for a given structure size (length and width) in view of limitof-detection optimization, noise consideration has to be studied.

We have also modeled the fluid-structure interaction using the Euler–Bernoulli beam model combined with the hydrodynamic force. This modeling shows good agreement with measurements when the rectangular structures are narrow and sufficiently long (length \geq 5 × width in our case). These results may help designers to

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optimize the cantilever geometry and dimensions in order to be more or less sensitive to the gas density variation depending on the application.

Moreover, due to the implementation of the phase linearization method [23] used to estimate the small natural frequency variation, detection of 2 mg/l of the gas mass density change has been achieved with all the microstructures and a limit of detection of 0.11 mg/l of the gas mass density variation (corresponding to a concentration of 100 ppm of H_2 in N_2) has been estimated, which is much smaller than the previous state-of-the-art value of 88 mg/l [7].

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7. References

- C. Vančura, Y. Li, J. Lichtenberg, K.U. Kirstein, A. Hierlemann, F. Josse, Liquid-phase chemical and biochemical detection using fully integrated magnetically actuated complementary metal oxide semiconductor resonant cantilever sensor systems, Analytical Chemistry, 79 (2007), pp 1646-1654.
- K. M. Goeders, J. S. Colton, L. A. Bottomley, Microcantilevers: Sensing chemical interaction via mechanical motion, Chemical review, 108 (2008), pp 522-542.
- A. Boisen, S. Dohn, S.S. Keller, S. Schmid, M. Tenje, Cantilever-like micromechanical sensors, Reports on Progress in Physics, 74 (2011) 036101.
- 4. Johnson, R. Mutharasan, Biosensing using dynamic-mode cantilever sensors: a review, Biosensors and bioelectronics, 32 (2012), pp 1-18.
- X. Li, D.W. Lee, Integrated microcantilevers for high-resolution sensing and probing, Measurement, Science and Technology., 23 (2012), 022001 (40 pages).

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- 6. Q. Zhu, Microcantilever sensors in biological and chemical detections, Sensors & transducers,125 (2011), pp 1-21.
- R. Rosario, R. Mutharasan, Piezoelectric excited millimeter sized cantilever sensors for measuring gas density changes, Sensors and Actuators B, 192 (2014), pp 99–104.
- S. Tétin, B. Caillard, F. Ménil, H. Debéda, C. Lucat, C. Pellet, I. Dufour, Modeling and performance of uncoated microcantilever-based chemical sensors, Sensors and Actuators B 143 (2010) 555–560.
- L. Zhao, L. Xu, G. Zhang, Z. Jiang, Y. Zhao, J. Wang, X. Wang, Z. Liu, Insitu measurement of fluid density rapidly using a vibrating piezoresistive microcantilever sensor without resonance occurring, IEEE sensors Journal, 14 (2014), pp 645-650.
- E. Lemaire, B. Caillard, M. Youssry, I. Dufour, High-frequency viscoelastic measurements of fluids based on microcantilever sensing: New modeling and experimental issues, Sensors and Actuators A, 201 (2013), pp 230–240.
- B. A. Bircher, L. Duempelmann, K. Renggli, H. P. Lang, C. Gerber, N. Bruns, T. Braun, Real-time viscosity and mass density sensors requiring microliter sample volume based on nanomechanical resonators, Analytical Chemistry, 85 (2013), pp 8676–8683.
- M.T. Boudjiet, V. Cuisset, C. Pellet, J. Bertrand, I. Dufour, Preliminary results of the feasibility of hydrogen detection by the use of uncoated silicon microcantilever-based sensors, International Journal of Hydrogen Energy (2014), http://dx.doi.org/10.1016/j.ijhydene.2014.03.228
- A. Kramer, Th. A. Paul, High-precision density sensor for concentration monitoring of binary gas mixtures, Sensors and Actuators A, 202 (2013), pp 52-56.
- D. Sparks, R. Smith, J. Patel, N. Najafi, A MEMS-based low pressure, light gas density and binary concentration sensor, Sensors and Actuators A, 171 (2011), pp 159–162.
- A. Loui, F.T. Goericke, T.V. Ratto, J. Lee, B.R. Hart, W.P. King, The effect of piezoresistive microcantilever geometry on cantilever sensitivity during surface stress chemical sensing, Sensors and Actuators A, 147 (2008), pp 516–521.

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- 16. H. Hocheng, W.H. Weng, J.H. Chang, Shape effects of micromechanical cantilever sensor, Measurement, 45 (2012), pp 2081–2088.
- 17. S. Subramanian, N. Gupta, Improved V-shaped microcantilever width profile for sensing applications, Appl. Phys. 42 (2009), 185501.
- M. Z. Ansari, C. Cho, Deflection, frequency, and stress characteristics of rectangular, triangular, and step profile microcantilevers for biosensors, Sensors, 9 (2009), pp 6046-6057.
- M. Narducci, E. Figueras, M. J. Lopez, I. Gràcia, J. Santander, P. Ivanov, L. Fonseca, C. Cané, Sensitivity improvement of a microcantilever based mass sensor, Microelectronic Engineering, 86 (2009), pp 1187– 1189.
- S. Morshed, B. C. Prorok, Enhancing the sensitivity of microcantileverbased sensors via geometry modification, Proc. SPIE 6223, Micro (MEMS) and Nanotechnologies for Space Applications, 62230S (2006), pp1-9.
- L.A. Beardslee, F. Josse, S.M. Heinrich, I. Dufour, O. Brand, Geometrical considerations for the design of liquid-phase biochemical sensors using a cantilever's fundamental in-plane mode, Sensors and Actuators B, 164 (2012), pp 7– 14.
- J.E. Sader, Frequency response of cantilever beams immersed in viscous fluids with applications to the atomic force microscope, Journal of applied physics, 84 (1998), pp 64-76.
- M.T. Boudjiet, J. Bertrand, C. Pellet, I. Dufour, New characterization methods for monitoring small resonant frequency variation: Experimental tests in the case of hydrogen detection with uncoated silicon microcantilever-based sensors, Sensors and Actuators B 199 (2014) 269–276.
- A. Maali, C. Hurth, R. Boisgard, C. Jai, T. C. Bouhacina, J.-P. Aimé, Hydrodynamics of oscillating atomic force microscopy cantilevers in viscous fluids, Journal of Applied Physics, 97 (2005), pp 074907-1-6.
- 25. R. D. Blevins, Formulas for natural frequency and mode shape, Van Nostrand Reinhold, 1979.
- 26. C. Bergaud, E. Cocheteau, L. Bary, R. Plana, and B. Belier, Formation of implanted piezoresistors under 100-nm thick for

nanoelectromechanical systems, Proc. 15th IEEE Int. Conf. Micro Electro Mech. Syst., (2002), pp 360–363.

 L. Fadel-Taris, C. Ayela, F. Josse, S.M. Heinrich, D. Saya, O. Brand, I. Dufour, Influence of non-ideal clamping in microcantilever resonant frequency estimation, FCS, Joint Conference of the IEEE International (2011), pp 1-5.

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