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Experimental Verification of Optimal Flux Weakening in Surface PM Machines Using Concentrated Windings

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# Abstract:

Previous analytical work has shown that it is possible to design surface PM (SPM) machines using fractional-slot concentrated windings to achieve wide speed ranges of constant power operation by satisfying the optimal flux-weakening condition. This paper presents a 6 kW 36-slot/30-pole concentrated winding prototype SPM machine that has been designed using a closed-form analytical technique developed specifically for this class of machines. Experimental testing of this machine has been carried out to determine its performance capabilities, including flux-weakening operation. Detailed comparisons between analytical, finite element analysis (FEA), and experimental results are presented that confirm the ability of fractional-slot concentrated winding SPM machines to achieve their high-speed operating objectives. Important issues including the machine's back-emf voltage at top speed, eddy current losses in the magnets, and inverter performance are analyzed and discussed in detail.

# SECTION I. Introduction

Past investigations have shown that wide speed ranges of constant-power operation can be achieved using surface PM (SPM) machines by introducing fractional-slot concentrated windings to reduce the machine's characteristic current [1]. A closed-form analytical technique has been developed that provides an effective means for rapidly analyzing candidate SPM machine designs using concentrated windings and tuning them to achieve the critical condition for optimal flux weakening [2].

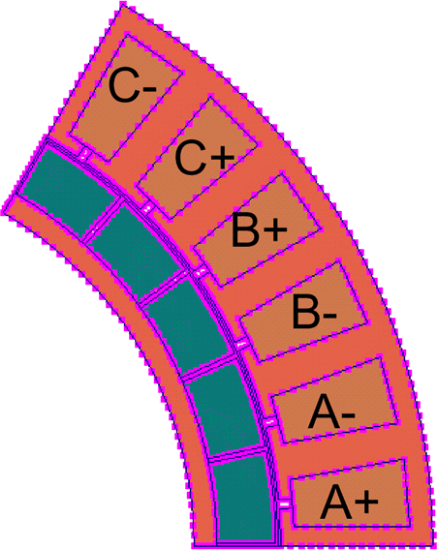
The ability of designers to use fractional-slot concentrated windings to reduce the SPM machine's characteristic current sufficiently to significantly expand the machine's high-speed operating capabilities has appeared only recently in the technical literature [3]. There are very few examples of experimental machines exhibiting these characteristics that have been tested and then documented in technical forums for the broad professional community [4].

This paper presents a 6kW 36-slot/30-pole concentrated winding prototype machine that has been designed using this analytical technique. Experimental testing of this machine has been carried out to evaluate its performance capabilities, including flux-weakening operation. Detailed comparisons between analytical, finite element analysis (FEA), and experimental results are presented in this paper. A wide range of the machine's parameters and operating characteristics are presented to help interested readers to assess the strengths and limitations of this class of machine. This discussion will include lessons learned by the authors - some unexpected - during the course of this development effort.

# SECTION II. Analytical and Finite Element Analysis Results

## A. Machine Dimensions and Parameters

A fractional-slot concentrated winding SPM machine has been designed for a wide speed range of constant-power operation using the analytical technique presented in [2]. A section of the 36-slot/30-pole machine (slot/pole/phase = 2/5) is shown in Fig. 1 [1]. The objective of this development effort has been to design the SPM machine to achieve a high constant power speed ratio (CPSR) with a target value of 10:1. Using the requirements for an automotive starter/alternator application as a reference point [5], the machine was originally designed as a motor to deliver 4kW at a base speed of 600 *r/min* and 6 kW at the top speed of 6000 *r/min*. All of the analytical results have been verified using finite element analysis (MagNet2D by Infolytica Corp.).

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**Figure 1:**Basic repeating unit of prototype SPM machine consisting of 6 stator slots and 5 poles

The basic machine unit consisting of 6 stator slots and 5 rotor poles is shown in Figure 1. Key parameters and dimensions for the machine stator and rotor are presented in Table I and Table II, respectively. Calculated inductance values for the machine are provided in Table III. Important machine parameters related to the machine's field weakening capabilities, including the rated and characteristic current values, are presented in Table IV. Table V provides information about the machine's mass, including a breakdown by material.

**TABLE I:**Stator Dimensions and Winding Data for The 36-SLOT/30-POLE SPM Machine

|  |  |  |  |
| --- | --- | --- | --- |
| Number of slots | 36 | Number of poles | 30 |
| Number of phases | 3 | Slots/pole/phase | 2/5 |
| Series turns | 108 | Number of turns/coil | 18 |
| Number of coils | 6 | Number of parallel oaths | 1 |
| Outer diameter | 280 [mm] | Active length | 60 [mm] |
| Total length | 72 [mm] | Slot fill factor | 35% |
| Slot opening width | 2 [mm] | Slot bottom width | I0 [mm] |
| Slot too width | 14.6[mm] | Slot opening height | 3 [mm] |
| Slot height | 25.4 [mm] | Back iron depth | 9 [mm] |
| Tooth width | 11.4 [mm] | Phase resistance | 63 [mΩ] |

**TABLE II:**Rotor Dimensions for the 36-SL0T/30-Pole SPM Machine

|  |  |  |  |
| --- | --- | --- | --- |
| Rotor outer radius | 88.6 [mm] | Magnets outer radius | 101.6 [mm] |
| Inner radius | 63.6 [mm] | Air gap thickness | 1 [mm] |
| Magnet depth | 13 [mm] | Magnet span | 11.4° [mech] |

**TABLE III:**Calculated Inductances for the 36-SLOT/30-Pole SPM Machine

|  |  |  |  |
| --- | --- | --- | --- |
| Self-inductance (including harmonic leakage) | 225[μH] | Mutual inductance (including harmonic leakage | ~0 |
| Self slot leakage inductance | 805[μH] | Mutual slot leakage inductance | ~0 |
| Total self inductance | 1.03[μH] | Net mutual inductance | ~0 |

**TABLE IV:**Calculated Current and Magnet Parameters for the 36-SL0T/30-P0Le SPM Machine

|  |  |  |  |
| --- | --- | --- | --- |
| Magnet Remanent Flux Density, | 0.55 [Tesla] @ 100°C | Magnet relative permeability, | 1.22 |
| RMS PM flux linkage | 34.8 [mWb-rms] | RMS Characteristic Current | 33.8 [Arms] |
| RMS Rated Current | 43 [ARMS] | Flux-Weakening Index | 0.79 |
| Copper Current density | 7 [ARMS/mm2] | Air Gap Shear stress | 3.1 [psi] -21 [kPa] |

**TABLE V:**Breakdown of Material Mass for the 36-SLOT/30-Pole SPM Machine

|  |  |  |  |
| --- | --- | --- | --- |
| Copper mass | 2.8 [kg] | Iron mass | 12.6 [kg] |
| Magnet mass | 3.6 [kg] | Total mass | 19 [kg] |

There are several important observations that can be made from the entries in these tables. Bonded neodymium-iron-boron magnets were selected for this prototype machine. The design value of the magnet remanent flux density  is 0.55 T with a relative permeability  of 1.22, using the magnet characteristics at 100°C in order to include temperature effects and to avoid demagnetization. The reason for choosing bonded magnets with a lower  value is to minimize the eddy-current losses in the magnets that will be discussed in more detail in Section III. The adoption of such relatively low-strength magnets explains the choice of a relatively large magnet depth of 13mm.

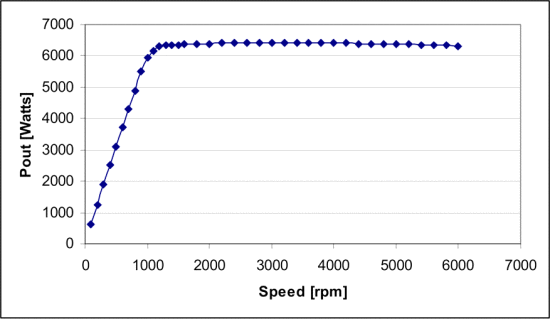
## B. Machine Inductances and Flux Weakening Operation

The self-and mutual inductance components in Table III (including harmonic leakage inductance) have been calculated using the winding function approach [6]. The slot leakage component is the dominant inductance component, attributable to the adoption of such a large effective air gap length (14mm).

It can be seen in Table IV that this machine has a calculated flux-weakening index *FWI* value (defined as the ratio of the machine's characteristic current  to its rated current ) that is less than unity (0.79) even though the design was initially tuned to achieve unity. This indicates that the machine deviates somewhat from the optimal flux-weakening condition, reflecting an oversight that occurred during the design process. More specifically, the slot leakage inductance was initially calculated using classical formulae that are appropriate for ac machines such as induction machines [7]. Unfortunately, such formulae become progressively inaccurate as the machine effective air gap increases, resulting in a calculated total phase self-inductance that is approx. 25% larger than the target value. It is noted, with some irony, that the design effort to increase the machine's inductance (in order to reduce the characteristic current) was *too* successful in this case.

Since discovering this error, more accurate 2-D models have been incorporated into the analytical model for calculating the slot leakage inductance in surface SPM machines with large effective air gaps [8]–[9][10]. Entries in both Tables III and IV are calculated using this improved model. This same model has been used to explore the changes that would be necessary in the machine lamination design to restore the *FWI* value to unity with the same rated current (43 Arms). A parametric study showed that, starting with the existing lamination, increasing the slot opening by 2mm (from 2 to 4mm) and reducing the slot opening height by 1 mm (from 3 to 2mm) changes the design characteristics sufficiently to meet the optimal flux-weakening condition. No other major modifications would be required to achieve this goal. However, a stator using this new lamination design has not been fabricated.

Updated analytical predictions for the prototype machine with the measured inductance (see Sec. VI) indicate that the required constant power level of 6 kW can still be achieved by increasing the dc bus voltage from 126 V to 195 V as shown in the calculated power vs. speed envelope curve in Fig. 2. This will be confirmed by experimental results later in this paper. The important observation is that this prototype machine continues to offer the opportunity to confirm that a wide constant-power speed range can be achieved despite its non-optimal characteristic current value.

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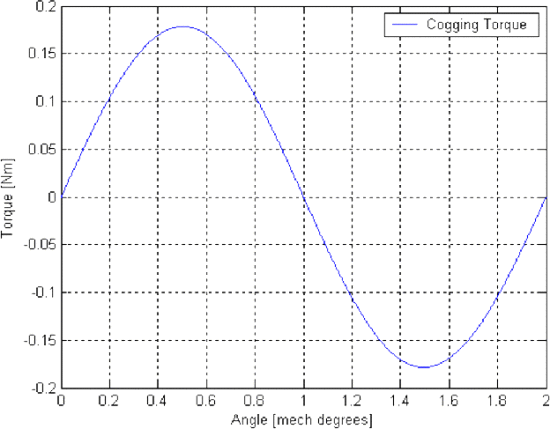
**Figure 2:**Calculated power vs. speed envelope of the prototype SPM machine

## C. Cogging Torque

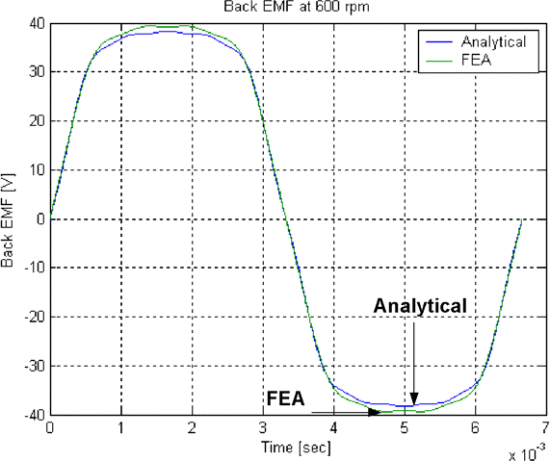
Figure 3 shows one cycle of the predicted cogging torque for the prototype 36s/30p SPM machine. The predicted peak-to-peak cogging torque amplitude is less than 1% of the rated torque. This result is consistent with results presented elsewhere in the literature [1],[11] [12]–[13] showing that cogging torque is one of the significant advantages of using fractional-slot concentrated windings.

## D. Finite Element Analysis Results

Figure 4 shows overlaid versions of the phase back-emf waveform at 600 *r/min* using both closed-form analysis and FEA. The excellent match between these two waveforms builds confidence in the accuracy of the analytical model. Although the phase back-emf waveform contains significant harmonic components, the triplen harmonics dominate so that little ripple torque is generated with three-phase sinusoidal current excitation. The line-to-line back-emf waveform is almost purely sinusoidal.

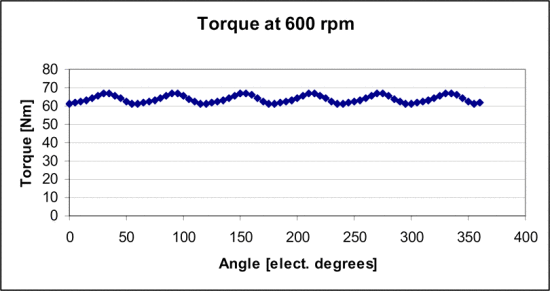
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**Figure 3:**One cycle of the predicted SPM machine cogging torque

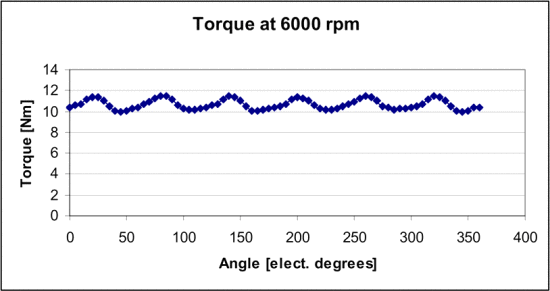
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**Figure 4:**Overlaid analytical and FEA predicted phase back-emf voltage waveforms at 600 r/min

The ability of the prototype machine to achieve the desired high CPSR value has also been verified using FEA. Figure 5 shows the predicted output torque at 600 *r/min* over one pole pair using sinusoidal current excitation. The peak-to-peak ripple torque is less than 9% and the average developed output power is more than 4 kW. The predicted output torque at *6000 r/min* under six-step voltage excitation is shown in Fig. 6, resulting in output power exceeding 6 kW.

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**Figure 5:**FEA predicted machine output torque at 600 r/min under sinusoidal current excitation.

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**Figure 6:**FEA predicted machine output torque at 6000 r/min under six-step voltage excitation

The machine inductance calculated using FEA is 1.16 mH, in comparison to a predicted value of 1.03 mH using the improved analytical model. The error is approx. 11% which is quite acceptable taking into consideration the difficulty of accurately estimating the slot leakage in a machine with such a large effective air gap length.

# SECTION III. Rotor Magnet Losses

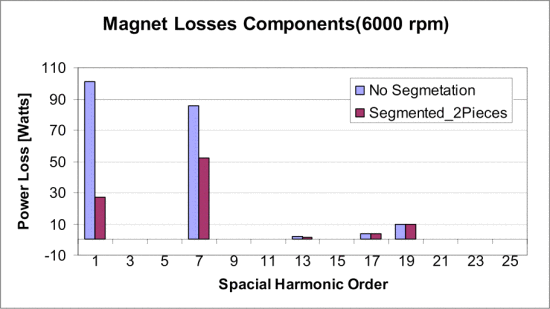
Since the fractional-slot concentrated winding produces an airgap magnetic flux distribution that is rich in spatial subharmonics and higher-order harmonics [1], one of the key performance issues in such machines is the resulting eddy-current losses induced in the magnets and rotor core [14].

In this prototype machine, the rotor core is laminated in order to minimize the eddy-current losses. The magnets selected for this machine are bonded NdFeB magnets that have a resistivity higher than 20 μΩm. Since bonded magnets have significantly higher resistivity than sintered magnets (0.5−1.5 ), the choice of bonded magnets is important for minimizing the magnet losses in this machine.

The tradeoffs associated with selecting the lower-strength bonded magnet material include an increase in magnet mass (due to the increase in magnet depth), and a slight increase in the machine rated current for the same rated torque. Both of these factors contribute to a slight decrease in the machine's specific torque density [Nm/kg] compared to a comparable SPM machine designed using high-strength sintered magnets.

The magnet losses have been evaluated using both closed-form analysis [14] and FEA. A good match has been achieved between the predicted losses using both techniques. The predicted average magnet losses at 6000 *r/min* is approximately 230 W which is less than 4% of the machine output at this speed. This result is an important factor in the machine's ability to achieve high machine efficiency (over 90%) at high speeds. The 6000 *r/min* operating point represent the highest magnet losses since these losses are proportional to the square of the speed [14].

An option for further reducing the eddy current losses is segmentation of the magnets along the rotor periphery. This option has been investigated both analytically and using FEA, and the results are summarized in Fig. 7. This figure confirms the expectation that the dominant spatial subharmonics (in this case the fundamental and the 7th) are the primary sources of the magnet losses. This figure also shows that segmentation has a significant effect on reducing the loss components generated by these dominant subharmonics.

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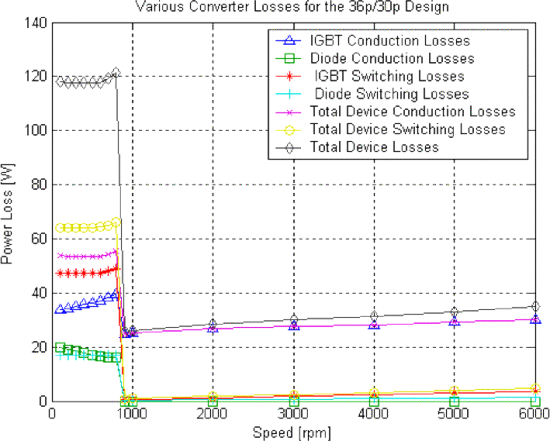
**Figure 7:**Predicted harmonic breakdown of magnet losses at 6000 r/min and the effect of segmentation.

# SECTION IV. Inverter Performance

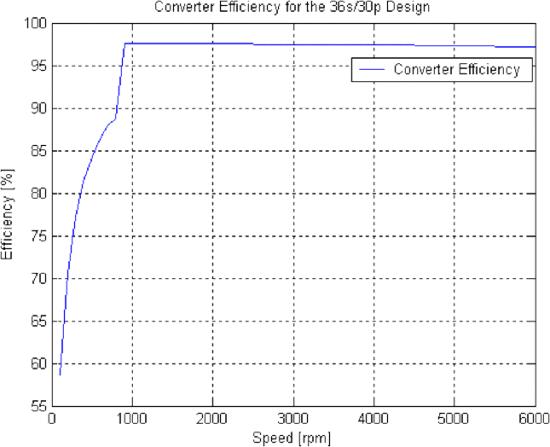
The high pole number of this prototype (30) raises some concerns regarding the inverter performance, particularly at high speeds. Performance characteristics of the inverter power stage while exciting the prototype SPM machine have been calculated, including an investigation of the impact of the machine's high pole number on converter losses [15], [16].

Since the minimum dc link voltage is approx. 200V, IGBTs were selected for the inverter switches. It is assumed that the inverter operates in PWM mode with a switching frequency of 20 kHz at all rotor speeds below the adjusted base speed of *800 r/min*, while six-step voltage excitation is applied at all higher speeds. As a result, the switching frequency equals the machine excitation frequency during high-speed operation.

The IGBT module used for this analytical exercise is manufactured by Fairchild Semiconductor [17] using *600V/75A* IGBTs. Figure 8 shows the predicted inverter loss components as a function of speed along the machine's capability envelope, while Fig. 9 shows the corresponding inverter efficiency. It can be seen that switch conduction losses dominate at high speeds, and the inverter efficiency exceeds 95% throughout the constant-power operating regime. Below the base speed, the switching losses are more prominent since the converter is still operating in its PWM mode.

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**Figure 8:**Predicted IGBT inverter loss components as a function of rotor speed along the machine capability envelope.

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**Figure 9:**Predicted inverter efficiency along the machine capability envelope as a function of rotor speed

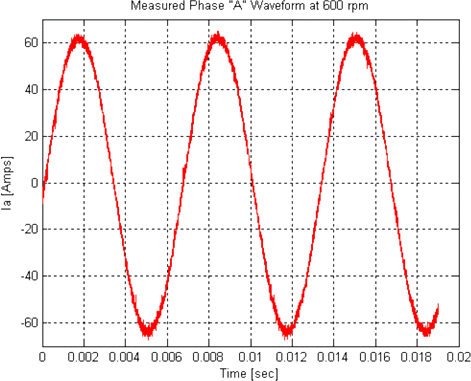
Another performance issue determined by the converter-machine interface is the amplitude of the phase current ripple. The maximum peak-to-peak current ripple amplitude can be estimated as follows [18]:

(1)

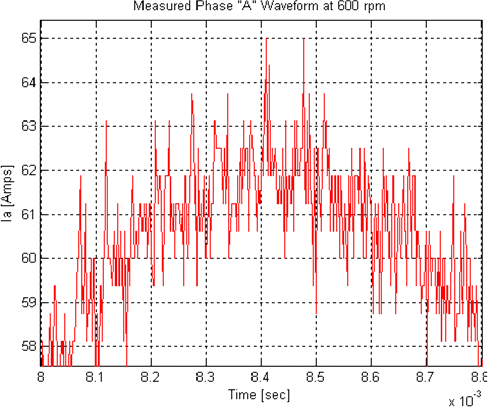
where  is the machine transient inductance, and  is the PWM switching period. This maximum ripple occurs when the machine phase is excited by a symmetrical square-wave voltage waveform (duty cycle=0.5) with period  and amplitude ·

For SPM machine designs with concentrated windings,  is equal to the machine phase self-inductance. For the prototype machine with a dc bus voltage of 300V and 20 kHz switching frequency, the predicted maximum current ripple is approx. 3A.

This value has been confirmed experimentally as shown in Figs. 10 and 11. Figure 10 shows the machine phase current at 600 r/min while Fig. 11 expands the interval where the maximum ripple occurs near the peak current. It can be seen that the current is quite sinusoidal and the peak-to-peak ripple is in the vicinity of 3A, as predicted. This ripple amplitude represents approx. 5% of the peak phase current which is quite acceptable. Additional calculations not presented here indicate that this low ripple contributes very little additional copper losses [19].

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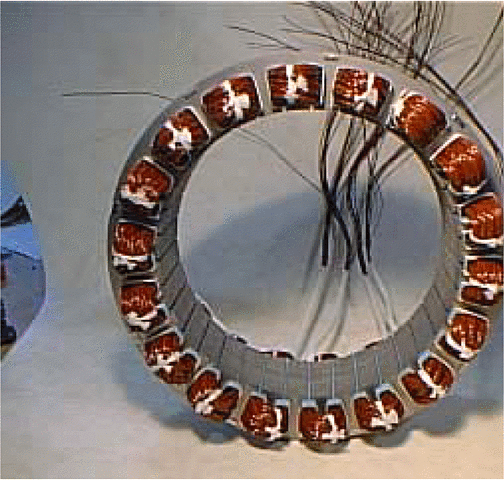
**Figure 10:**Measured phase current at 600 r/min with rated current operation.

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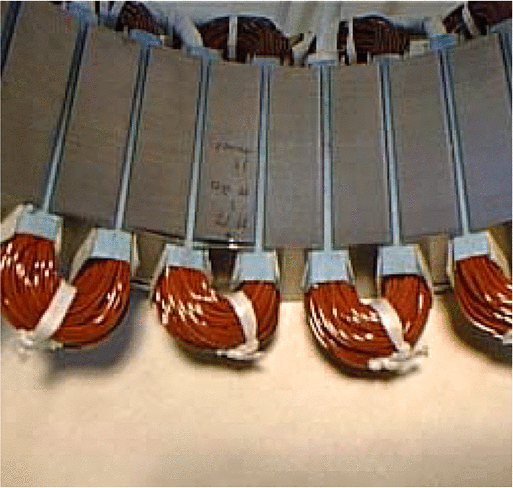
**Figure 11:**Expanded view of measured phase current at 600 r/min showing peak ripple.

# SECTION V. Prototype Machine Fabrication & Test Configuration

This section provides information about the prototype machine fabrication and test configuration. Figure 12 shows the laminated stator core and the concentrated winding coils. The stator lamination stack is held together using cleats. The thin back iron made possible by the high number of poles is also evident. Figure 13 highlights the concentrated stator windings and their short non-overlapping end turns.

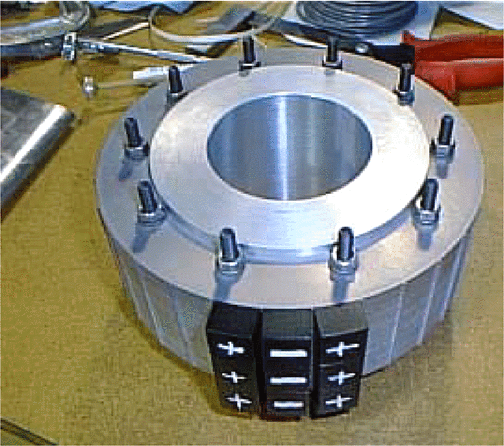
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**Figure 12:**Prototype machine stator core and concentrated stator windings

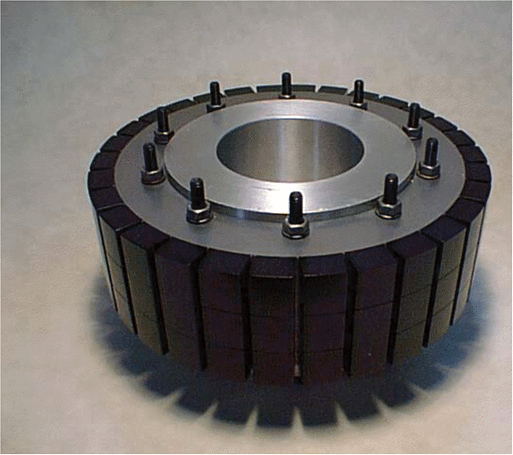
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**Figure 13:**Close-up view of concentrated winding with nonoverlapping end turns

Figure 14 shows the rotor assembly during fabrication including the aluminum inner hub, the rotor laminated core, and three of the assembled magnet poles. The rotor laminations are held together using axial bolts. The magnets are positioned on the rotor surface with the aid of small location guides on the periphery of the rotor laminations. The magnets are then fixed in place using glue and two layers of fiberglass tape. Each pole is divided axially into 3 magnet pieces due to magnet manufacturing limitations. Figure 15 shows the rotor after all the magnets were mounted.

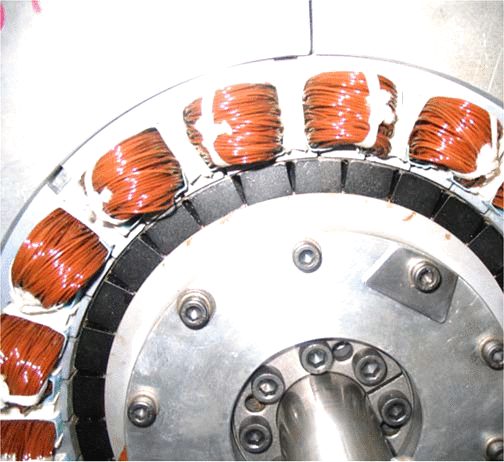
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**Figure 14:**Rotor magnets during the assembly process

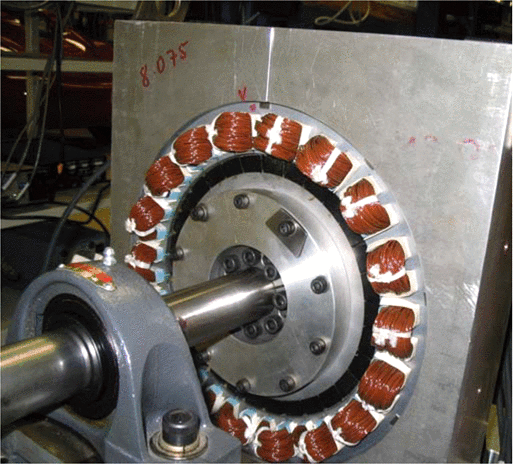
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**Figure 15:**Rotor assembly showing hub, laminations, and mounted magnets

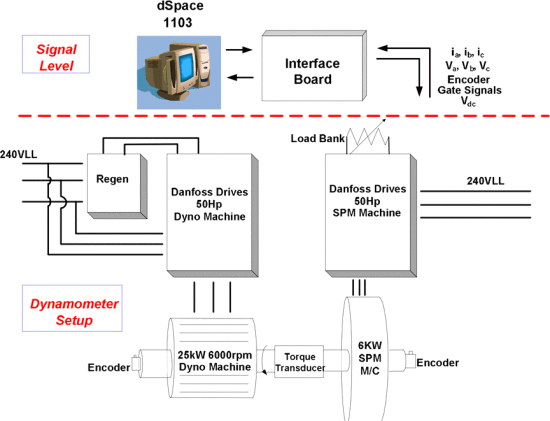
Figures 16 and 17 show two different views of the prototype machine. In these figures, the stator has been installed inside the aluminum C-Core open frame. The rotor has also been mounted on the shaft and the bearings are visible in Fig. 18.

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**Figure 16:**Close-up view of the machine after stator-rotor assembly in frame

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**Figure 17:**End view of the machine after assembly, including bearings.

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**Figure 18:**Dynamometer test configuration for prototype SPM machine [20]

A schematic of the test configuration is shown in Fig. 18 [20]. The prototype 6 kW SPM machine is coupled to a flexible 4-quadrant dynamometer that uses a 25kW, 6000 r/min induction machine. An in-line torque transducer is used to measure the torque and speed. Each machine is excited by a 50 hp Danfoss drive controlled using a dSpace 1103 board.

# SECTION VI. Experimental Results

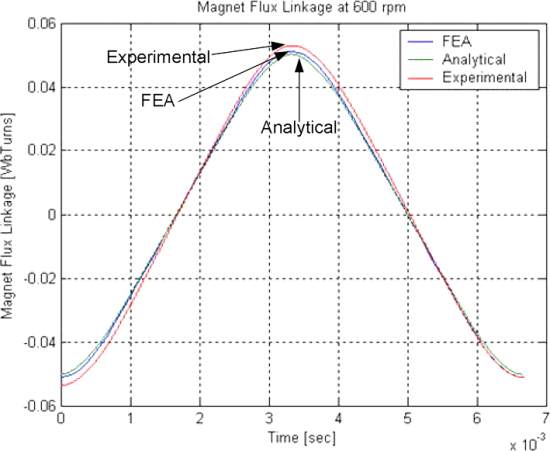
This section provides a summary of the key experimental results, including parameter measurements and comparisons between the experimental results and both the closed-form analytical and FEA results.

## A. Machine of Parameters

The measured value of the stator phase resistance at room temperature is approx. , 11% higher than the analytical prediction of . The main reason for this discrepancy is the difference between the 40% copper slot fill factor used in the calculations and the actual achieved value of approx. 35%.

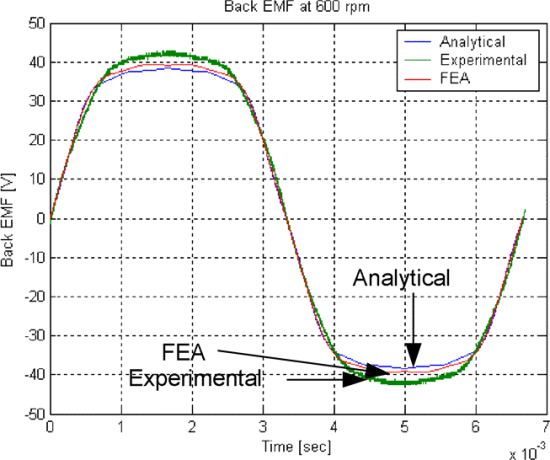
The measured phase inductance is approx. 1.3 mH which is higher than both the updated analytical prediction (1.03 mH) and the FEA prediction (1.16 mH). Sources of this difference include the end leakage inductance that is not included in either the 2D FEA or the analytical predictions, and remaining inaccuracies in the slot leakage inductance estimate.

Figure 19 shows the measured phase  magnet flux linkage compared to both the analytical and FEA results, demonstrating very good matches in both cases. The experimental flux linkage is slightly higher than either of the analytical results due to the fact that the actual magnet  value of the received magnets is approx. 0.59T at room temperature compared to the magnet  design value of 0.55T at 100°C.

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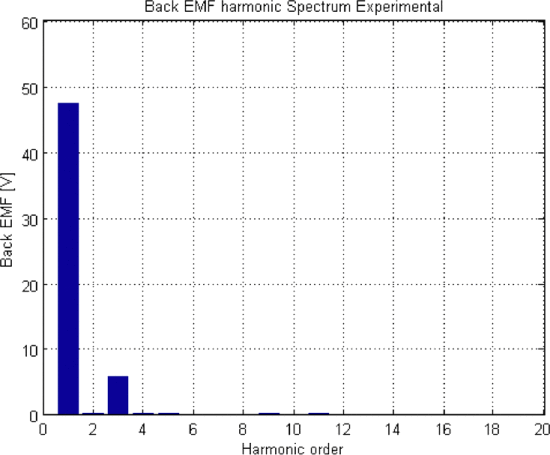
**Figure 19:**Comparison of calculated and measured phase  magnet flux linkage waveforms

Figure 20 shows the measured phase A back-emf voltage compared to both the closed-form analytical and FEA results, again demonstrating very good matches. As in the case of the flux linkages, the slightly elevated amplitude of the experimental back-emf is attributable to the difference in .

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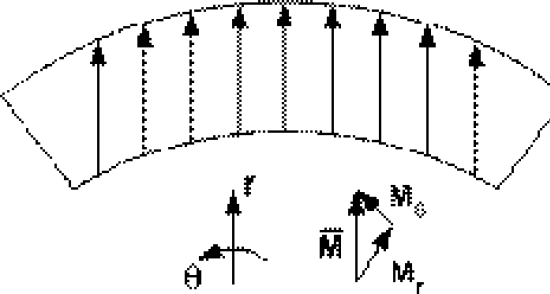
**Figure 20:**Comparison of calculated and measured phase  back-emf voltage waveforms at 600 r/min

The measured harmonic spectra of the experimental back-emf waveform is shown in Fig. 21. It can be seen that the measured back-emf waveform consist almost entirely of a fundamental and a 3rd harmonic component. The analytical back-emf waveform includes some higher-order harmonic components in addition to the fundamental and 3rd harmonic components. This favorable result suggests that the prototype machine will have lower torque ripple than predicted. With a floating neutral winding connection, the 3rd harmonic component in the back-emf voltage is prevented from contributing any ripple torque since triplen harmonic currents cannot flow.

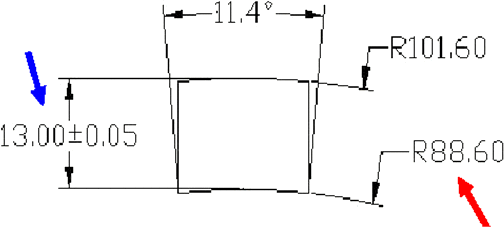
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**Figure 21:**Harmonic spectrum of the measured phase A back-emf voltage waveform at 600 r/min

The small difference between the measured and predicted back-emf harmonic spectra can be explained by comparing the magnets shape used in the analytical model shown in Fig. 22 [21] and the actual magnet shape used in the prototype machine shown in Fig. 23. While parallel magnetization is used in both cases, the edges of the actual magnet are slightly tapered compared to the assumed analytical shape due to manufacturing constraints. This tapered magnet shape is responsible for the near-absence of higher-order harmonics in the measured back-emf voltage waveform.

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**Figure 22:**Shape of the magnets used in the analytical model

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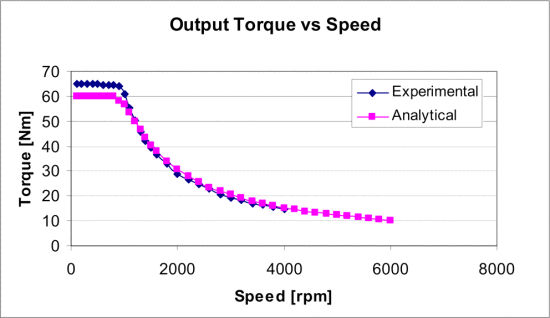
**Figure 23:**Actual shape of the magnets used in the prototype machine

## B. Machine Torque and Power vs. Speed Envelopes

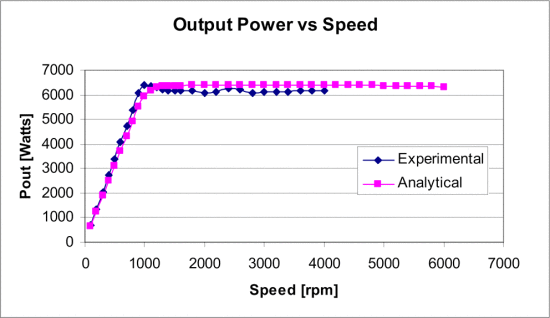
As discussed previously in Section II, the dc bus voltage was raised from its original design value of 126V to 195V as a result of the higher-than-expected phase inductance. This higher bus voltage makes it possible to demonstrate that the machine can achieve a wide speed range of constant-power operation at the 6 kW level.

For the test results reported here, the bus voltage was raised to a somewhat higher value than the minimum required value of 195V, and the tests were conducted with the machine operating continuously in PWM mode in order to simplify the control issues. The torque/power envelope tests were carried out by adjusting the synchronous-frame  and  current values to develop the desired torque/power within the targeted phase voltage limit of 87.8 Vrms (fundamental). This phase voltage corresponds to a dc link bus voltage of 195V (ignoring switch voltage drops) with six-step voltage excitation (i.e., ).

Comparisons of the measured and updated analytical machine torque vs. speed envelopes and the corresponding power vs. speed envelopes are shown in Figs. 24 and 25, respectively. The envelope curves in Figs. 24 and 25 show that there is a very good match between the measured and analytical results up to the maximum test speed of 4000 r/min. These results are very significant since they confirm that the prototype machine has achieved a wide speed range of constant-power operation (approx. 5:1, to date).

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**Figure 24:**Comparison of the measured and calculated machine torque vs. speed envelopes

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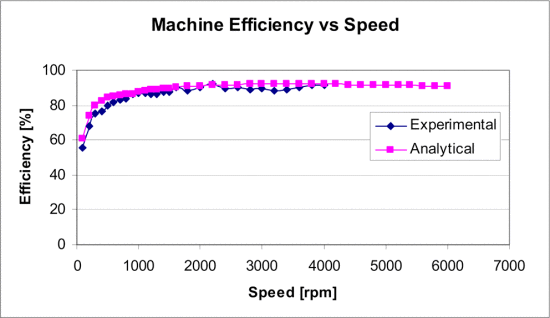
**Figure 25:**Comparison of the measured and predicted machine power-speed envelopes

At the time of this writing, no tests have been carried out above 4000 r/min in order to complete testing at lower speeds before exposing the rotor to higher structural stresses. All available evidence suggests that the machine will be able to demonstrate higher CPSR values before testing is completed.

The results in Fig. 24 show that the measured torque is slightly higher than predicted at lower speeds for the same stator current. This is consistent with the higher value of magnet  in the prototype machine, as previously discussed.

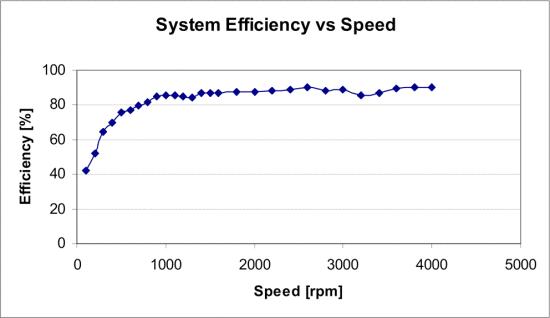
## C. Machine and Inverter Efficiency vs. Speed Envelopes

Figure 26 shows a comparison of the measured and calculated machine efficiency vs. speed along the maximum torque/power envelope. Updated analytical predictions and measured results agree very closely over the entire tested speed range up to 4000 r/min. The measured prototype machine efficiency is higher than 90% at elevated speeds, confirming successful suppression of the eddy current losses in the magnets and rotor core that are generated by the significant airgap subharmonic field components. This is very significant since these losses have been considered to be one of the key potential obstacles to using fractional-slot concentrated windings for high-speed operation.

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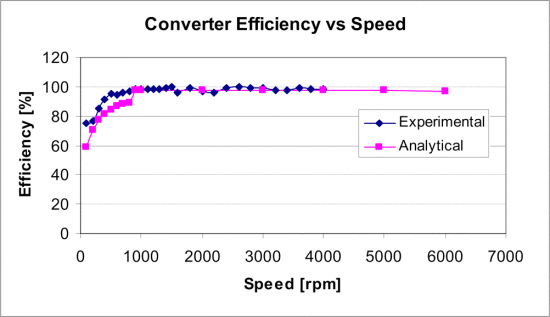
**Figure 26:**Comparison of the measured and calculated machine efficiency vs. speed envelopes

Figure 27 shows the measured machine-plus-inverter system efficiency vs. speed envelope. The inverter input power was determined using measurements of the dc bus voltage and current. The output power was determined by measuring the machine output torque and speed. This curve shows that the machine-plus-inverter efficiency is nearly 90% over most of the speed range up to 4000 r/min, confirming the opportunities provided by the concentrated winding SPM machine to achieve high drive efficiency values.

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**Figure 27:**Measured machine-plus-inverter system efficiency vs. speed envelope

Using the measured machine and system efficiency values presented in the preceding two figures, the “measured” converter efficiency has been extracted and compared to the analytical predictions in Fig. 28. Consistent with the results in Figs. 26 and 27, the predicted and measured inverter efficiency values agree very well, reaching values in the vicinity of 98% at high speeds.

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**Figure 28:**Comparison of the measured and calculated inverter efficiency vs. speed envelopes

# SECTION VII. Conclusions

A 6 kW 36-slot/30-pole fractional-slot concentrated winding SPM machine has been successfully designed, fabricated, and tested to achieve a wide speed range of constant-power operation. Closed-form analysis and FEA have been used extensively during the design process. Important machine and drive performance issues including the eddy current losses in the magnets and the inverter losses have been analyzed in detail.

Experimental results from the prototype SPM machine were used to improve the accuracy of the closed-form analytical model for machine inductance calculations. Comparisons between the machine parameters and performance derived from the improved analytical model, FEA, and the experimental tests have demonstrated very good agreement.

The test results have convincingly demonstrated the SPM machine's ability to deliver wide speed ranges of constant-power operation as well as high machine efficiency. These experimental verification results are intended to assist PM machine and drive designers who are interested in considering SPM machines for applications such as electric traction that have generally been considered beyond its reach in the past.

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